



UNIVERSITÀ DEGLI STUDI DI PALERMO

DEPARTMENT	Matematica e Informatica
ACADEMIC YEAR	2021/2022
BACHELOR'S DEGREE (BSC)	MATHEMATICS
SUBJECT	PROBABILITY THEORY
TYPE OF EDUCATIONAL ACTIVITY	B
AMBIT	50195-Formazione Modellistico-Applicativa
CODE	01736
SCIENTIFIC SECTOR(S)	MAT/06
HEAD PROFESSOR(S)	SANFILIPPO GIUSEPPE Professore Ordinario Univ. di PALERMO
OTHER PROFESSOR(S)	
CREDITS	6
INDIVIDUAL STUDY (Hrs)	94
COURSE ACTIVITY (Hrs)	56
PROPAEDEUTICAL SUBJECTS	01249 - MATHEMATICAL ANALYSIS 1
MUTUALIZATION	
YEAR	3
TERM (SEMESTER)	1° semester
ATTENDANCE	Not mandatory
EVALUATION	Out of 30
TEACHER OFFICE HOURS	<p>SANFILIPPO GIUSEPPE</p> <p>Wednesday 17:30 19:30 Canale Teams, https://teams.microsoft.com/l/team/19%3a743165a223bc4c069089c244ea5a0756%40thread.ta%20conversations?groupId=d07526b2-8d64-4ab6-bce0-442348453e65&tenantId=bf17c3fc-3ccd-4f1e-8546-88f06b912345 Si prega di prenotare il ricevimento tramite email</p> <p>Thursday 09:00 10:00 DMI, Via archirafi 34, secondo piano. Prenotare il ricevimento per email</p>

PREREQUISITES	<p>Combinatorics. Analytic geometry. Linear systems. Set theory. Sequences and series. Differential and integral calculus. Complex numbers.</p>
LEARNING OUTCOMES	<p>1) KNOWLEDGE AND UNDERSTANDING The student should know the following topics: - Elements of logic and combinatorics; - Various concepts of probability - Setting of Coherence - Elementary Probability; - Events and conditional events; - Random quantities and probability distributions; - Summary statistics; - Classical problems of probability. - Random vectors, joint and marginal probability distributions; - Functions of random quantities and of random vectors; - Relations among random quantities; - Some limit theorems.</p> <p>2) APPLYING KNOWLEDGE AND UNDERSTANDING The student should know how to exploit probabilistic tools to reasoning under uncertainty. In particular, the student should be able to: - Describe the uncertainty; - Check the coherence of a probability assessment on an arbitrary finite family of events; - Apply Bayes' rule and compound probability theorem; - Solve classical problems of probability; - Select the suitable probability distribution to describe some standard random problems; - Apply limit theorems; - Compute marginal probability distributions from joint probability distributions. - Solve problems involving functions of random quantities.</p> <p>3) MAKING JUDGEMENTS Being able to motivate the choice of some probabilistic tools and models in order to properly study some problems under partial or incomplete knowledge.</p> <p>4) COMMUNICATION. The student should know how to illustrate in a clear and coherent way the description and the analysis of a random problem to both expert and non-expert people.</p> <p>5) LIFELONG LEARNING SKILLS. Being able to exploit the power of self-discovery, exploration, learning and mastery. In particular the student should be able to deep some well-known notions in probability theory and to discover new notions by studying from other research books or from research articles.</p>
ASSESSMENT METHODS	<p>The exam is composed by a written test (or two intermediate written tests) followed by an oral test Written tests The written test will be composed of 4 exercises: 2 exercises which mainly concern topics of the first half of the course and 2 exercises which mainly concern topics of the second half of the course. A mark of 7.5 points will be given for each exercise correctly solved. The evaluation of the written test will be made by means of a 30-point scale. Candidates who do not pass the written test are encouraged to repeat the written test.</p> <p>Intermediate written tests. The first intermediate written test will be composed of 2 exercises which mainly concern topics of the first half of the course. The second intermediate written test will be composed of 2 exercises which mainly concern topics of the second half of the course. A mark of 15 points will be given for each exercise correctly solved. The evaluation of the intermediate written test will be made by means of a 30-point scale. Those who pass both intermediate written tests will avoid the written test and will receive as score of the written test the average of the two intermediate scores. Some solved tests will be made available during the lectures. The written tests are designed in order to evaluate the degree of knowledge and the ability of the candidate to solve problems similar to those illustrated during</p>

	<p>the lectures and during practicals. In particular, through them it will be possible to measure the ability of the candidate in order to: formalize a random phenomenon; motivate the choice of a probabilistic model and of some probability distributions; provide summary statistics; understand conditionalization; apply or re-elaborate theoretical results; apply limit results; exploit standard normal table; apply mathematical tools to solve random problems.</p> <p>Oral Test By starting from a deepening on the written test, the oral test, through the formulation of some questions, will be used to evaluate the degree of knowledge of the student in some theoretical results and in the use of technical language. The score of the oral test will be a number usually belonging to the set $\{-4, -3, -2, -1, 0, 1, 2, 3, 4\}$. The score of the oral test will be used to finalize and / or improve the grade obtained in the written tests.</p> <p>Finale grade By setting S="the score of the written test" and O="the score of the oral test", the final grade V usually will be $V=\min(S+O, 30)$, if $S+O>0$ or $V=0$ otherwise. The student pass the exam if the final grade is greater or equal than 18/30 The minimum grade 18/30 in order to pass the exam will be given to the student that knows the basic fundamentals of the course, that is able to do some links among the different topics and that is able to use technical language. The maximum grade 30/30 cum laude will be given to the student that fully reaches the learning outcomes and that gets a score $S+O$ greater than 30.</p>
EDUCATIONAL OBJECTIVES	<p>Being able to describe and represent some theoretical and real random problems through suitable probabilistic models, by eventually using R or Python. In particular, the student should be able to: -motivate the choice of some probability distributions; provide the summary statistics; -properly assess degrees of believe to (conditional or simple) events; update probability; -exploit theoretical results for the study and analysis of random vectors. The student should also know how to solve some "classical paradoxes" by means of the elementary notions of probability.</p>
TEACHING METHODS	<p>Lectures and practicals. Usually, theory will be explained in the lecture and then applied and tested in the practical class. An english paper on probability or a book chapter will be shared with the students.</p>
SUGGESTED BIBLIOGRAPHY	<p>Testi di riferimento (References) - [1] Sheldon Ross; Calcolo delle Probabilita' 3a ed.; Apogeo Education - Maggioli Editore, 2013; ISBN 9788838788604 (English version: A first course in Probability, 8th edition, Pearson) - [2] Romano Scozzafava; Incertezza e Probabilita'; Zanichelli, 2003; ISBN: 9788808079756</p> <p>Dispense Materiale didattico e soluzioni dei compiti di esami forniti dal docente (Notes and exercises provided by the Teacher).</p> <p>Per alcuni argomenti del programma dell'insegnamento, non presenti nei testi consigliati, vengono forniti i seguenti riferimenti bibliografici. (For some particular topics of the syllabus proper references are given below).</p> <p>- [3] Paolo Baldi; Calcolo delle Probabilita'; McGraw-Hill, 2011, ISBN 978-8838666957; - [4] Bruno de Finetti; Teoria delle Probabilita'; Giuffre', 2005 (ristampa), ISBN 978-8832821758; (English version of the book: Theory of Probability: A critical introductory treatment, Wiley, 2017, ISBN 978-1119286370) - [5] Luciano Daboni; Calcolo delle Probabilita' ed Elementi di Statistica; Utet, 1981, ISBN 978-8877502087. - [6] Giorgio Dall'Aglio; Calcolo delle Probabilita'; Zanichelli, 2001, ISBN: 9788808176769. - [7] Giuseppe Espa, Rocco Micciolo, Problemi ed esperimenti di statistica con R, Apogeo, 2014, ISBN 978-8838786105. - [8] Kevin Ross & Dennis L. Sun (2019) Symbluate: Simulation in the Language of Probability, Journal of Statistics Education, 27:1, 12-28, DOI: 10.1080/10691898.2019.1600387</p>

SYLLABUS

Hrs	Frontal teaching
2	Historical notes. Chevalier de Mere's Problem ([6]). Events, indicators, logical operations and relations ([2,5]). De Morgan's Law. Basic notions on combinatorial Analysis. Binomial theorem. Cardinality of a finite power set. Finite partition of the sure event. The classical interpretation of probability. Basic properties of probability.
2	The main Interpretations of probability:: classical, axiomatic ([3]), frequency, subjective ([2]). Betting criterion and coherence principle ([2]). Probability and measure theory ([3]). Characterization of coherence.
2	Conditional events and conditional probability [2]. Properties of conditional probability [1]. Compound probability theorem. Disintegration law. Bayes' rule. Events which are regarded stochastically independent.
5	Simple Random quantities [2]. Urn problems. Extraction of white balls, given n draws with replacement in an urn with a known number of black and white balls. Binomial distribution. Extraction of white balls, given n draws without replacement in an urn with a known number of black and white balls. Hypergeometric distribution. Mixture of binomial distributions [2]. Mixture of hypergeometric distributions Exchangeability. Expected value and variance of a simple random quantity.
4	Discrete probability. Properties of expectation and variance. Cumulative distribution and discrete random quantities. Poisson and geometric distribution. Binomial approximation. Property of memoryless of the geometric distribution. Pascal and negative binomial distribution [2]. Markov's inequality. Chebyshev's inequality.
5	Infinity and probability. Continuous random quantities. Density [2,3], cumulative distribution function, expectation, variance. Property of continuous random quantities. Some continuous distributions: Uniform, Exponential, Normal, Gamma, Beta, Chi-square, Laplace, Power law, etc. Hazard rate function [1,2]. Survival function. Memoryless property of exponential distribution.
6	Discrete and continuous random vectors. Cdf, joint distribution functions, marginal distributions, conditional distributions. Independence. Property of expectation. Covariance. Pearson correlation coefficient. Covariance matrix. Linear regression. Normal distribution. Distribution of function of random quantities [see also 3]. The cumulative distribution function (cdf) technique.
3	Characteristic function [2,3,6] (or in alternative moment generating function [1]) and properties. Sum of random quantities. Convolution operator. General Chi-square distribution.
3	Convergences of random quantities (see also [3,6]). Limits theorem. Central limit theorem. Normal approximation of binomial distribution. Weak law of large numbers.
Hrs	Practice
2	Preliminaries notion of combinatorial analysis. Logical operations among events. Properties of probability.
4	Constituents associated with a family of n events. Decomposition formula. Events logically independent. Properties of probability and coherence principle. Coherence checking. Probability and (decimal) odds gambling.
3	Conditional probability. Bayes rule. Paradoxes in probability theory.
3	Discrete probability. Basic discrete probability distributions in R [7].
4	Continuous random quantities. Summary statistics. Survival analysis.
4	Random vectors. Distribution of function of random quantities.
4	Normal distribution. Limits Theorem. Characteristic function (or generating moment function)