

# UNIVERSITÀ DEGLI STUDI DI PALERMO

| DEPARTMENT     Ingegre       ACADEMIC YEAR     2020/20 |                                                              |
|--------------------------------------------------------|--------------------------------------------------------------|
|                                                        |                                                              |
|                                                        | 21                                                           |
| BACHELOR'S DEGREE (BSC) BUILDI                         | NG ENGINEERING, INNOVATION AND RETROFITTING                  |
| INTEGRATED COURSE MATHE                                | MATICAL ANALYSIS - INTEGRATED COURSE                         |
| <b>CODE</b> 19109                                      |                                                              |
| MODULES Yes                                            |                                                              |
| NUMBER OF MODULES 2                                    |                                                              |
| SCIENTIFIC SECTOR(S) MAT/05                            |                                                              |
| HEAD PROFESSOR(S) TORNA                                |                                                              |
| OTHER PROFESSOR(S) TRIOL                               | D SALVATORE Professore Associato Univ. di PALERMO            |
| TORN/<br>ELISAE                                        |                                                              |
| CREDITS 12                                             |                                                              |
| PROPAEDEUTICAL SUBJECTS                                |                                                              |
| MUTUALIZATION                                          | EMATICAL ANALYSIS - MODULE 1 - Corso: INGEGNERIA CIVILE      |
| MATHE                                                  | MATICAL ANALYSIS - MODULE 1 - Corso: CIVIL ENGINEERING       |
| YEAR 1                                                 |                                                              |
| TERM (SEMESTER) Annual                                 |                                                              |
| ATTENDANCE Not ma                                      | ndatory                                                      |
| EVALUATION Out of 3                                    | 0                                                            |
| TEACHER OFFICE HOURS TORNA                             |                                                              |
| Tuesday                                                | 9:30 10:30 Studio del docente                                |
| TRIOLO                                                 | SALVATORE                                                    |
| Wednes                                                 | day 10:00 12:00 Dip Metodi e modelli matematici primo piano. |

DOCENTE: Prof.ssa ELISABETTA TORNATORE

| DOCENTE: Prof.ssa ELISABETTA TOI<br>PREREQUISITES |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
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| · · · · · · · · · · · · · · · · · · ·             | Typical high school sillabus                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
| LEARNING OUTCOMES                                 | <ul> <li>-Knowledge and understanding</li> <li>The student must know and understand the basic concepts of the course. Know and be able to work in different numerical sets, know, understand and be able to apply knowledge relating to succession, elementary functions, limit of sequences and functions, differential and integral calculus.</li> <li>-Applying knowledge and understanding</li> <li>The student will be able to use mathematical language, apply the acquired knowledge in solving proposed problems and generally include the use of mathematical methods in the applied sciences.</li> <li>-Making judgment</li> <li>At the end of the course the student will have specific knowledges in identifying the most relevant technical solutions in relation to different problems. at the same time understand how to use the knowledge acquired in the study of other disciplines.</li> <li>-Communication skill</li> <li>During lectures and exercises the student will be urged to interact with relevant questions to clarify any doubts and to develop capacity to apply the techniques learned to other scientific subjects.</li> <li>-Learning ability</li> <li>Ability to attend, using the knowledge acquired in the course.</li> <li>Knowledge of the differential and integral calculus for functions of one real variables. The student will be able to study of the graphs of elementary functions, to solve integration problems of elementary character, to discuss the nature of numerical sequences, to state and prove basic theorems of Mathematical Analysis.</li> </ul> |
| ASSESSMENT METHODS                                | <ul> <li>The written exam consists of exercises. The written exam is evaluated in the following form : A, B, C, D, E, F. The oral exam consists of questions and proofs on the theory presented in the course. In addition, based on the written exam, we can be required clarifications on errors and resolutions of exercises.</li> <li>The final vote will be given in thirtieths.</li> <li>(rating 30-30L): Excellent knowledge of subjects and theories addressed in the course; excellent level of awareness and autonomy in the application of theories to solve problems;</li> <li>(rating 26-29) : Good knowledge of subjects and theories addressed in the course; good degree of awareness and autonomy in the application of theories to solve problems;</li> <li>(rating 24-25): Good knowledge of subjects and theories addressed in the course; fair degree of awareness and autonomy in the application of theories to solve problems;</li> <li>(rating 21-23); fair knowledge of subjects and theories addressed in the course; sufficient degree of awareness and autonomy in the application of theories to solve problems;</li> <li>(rating 18-20): sufficient knowledge of subjects and theories addressed in the course; sufficient degree of awareness and autonomy in the application of theories to solve problems;</li> </ul>                                                                                                                                                                                                                                                         |
| TEACHING METHODS                                  | The course is annual, divided into two modules, taking place in the two teaching periods<br>of the first year: the first module in the first semester, the second module in the second semester. Teaching is provided through lectures and exercises.<br>At the end of each teaching module there is a written test in progress,<br>. Passing these tests in progress can exempt the student<br>completely or only partially, from<br>final written test.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |

#### MODULE MATHEMATICAL ANALYSIS 2

#### Prof. SALVATORE TRIOLO

#### SUGGESTED BIBLIOGRAPHY

 Bertsch Dal Passo Elementi di Analisi matematica 2

 Bramanti Pagani Salsa Calcolo infinitesimale e Algebra lineare.

 AMBIT
 50106-Formazione scientifica di base

 INDIVIDUAL STUDY (Hrs)
 98

 COURSE ACTIVITY (Hrs)
 52

 EDUCATIONAL OBJECTIVES OF THE MODULE

 At the end of the course the student will acquire the knowledge on the main

topics, methodologies on infinitesimal differential calculus for functions of two or more variables. In particular, the student will be able to understand the issues arising from the needing to create a rigorous language using the logical-deductive method to deal with intuitively simple math problems. The students will be also able to understand simple physical problems and to convert them in the correct mathematical language, for instance through differential equation.

## SYLLABUS

| Hrs | Frontal teaching                                                                                                    |
|-----|---------------------------------------------------------------------------------------------------------------------|
| 1   | Objectives of the discipline.                                                                                       |
| 3   | Sequences of functions. Power series.                                                                               |
| 2   | Topology of the real vector space R^n.                                                                              |
| 2   | Differential equations.                                                                                             |
| 5   | Limits for functions of multiple real variables: definitions,main properties and theorem. Continuity of a function. |
| 5   | Differential calculus for functions of multiple real variables.                                                     |
| 5   | Integration theories.                                                                                               |
| 5   | Differential calculus.                                                                                              |
| Hrs | Practice                                                                                                            |
| 5   | Sequences of functions. Power series.                                                                               |
| 4   | Differential equations.                                                                                             |
| 5   | Differential calculus.                                                                                              |
| 5   | Integration theories.                                                                                               |
| 5   | Conservative and non conservative fields. Work of a conservative field.                                             |

### MODULE MATHEMATICAL ANALYSIS 1

Prof.ssa ELISABETTA TORNATORE

## SUGGESTED BIBLIOGRAPHY

| SUGGESTED BIBLIOGRAPHY                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                             |  |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|
| M. Bertsch, R. Dal Passo, L. Giacomelli, Analisi Matematica (2Ed) McGraw-Hill                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                                                                                                                                                             |  |
| Per Approfondimenti:<br>M. Bramanti, C. Pagani, S. Salsa Analisi Matematica I<br>P. Marcellini, C. Sbordone , Elementi di Analisi Matematica I Li<br>Per le esercitazioni:<br>C. Marcelli, Analisi matematica 1 esercizi con richiami di teoria                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | -                                                                                                                                                                                                           |  |
| AMBIT                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 50106-Formazione scientifica di base                                                                                                                                                                        |  |
| INDIVIDUAL STUDY (Hrs)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 98                                                                                                                                                                                                          |  |
| COURSE ACTIVITY (Hrs)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 52                                                                                                                                                                                                          |  |
| EDUCATIONAL OBJECTIVES OF THE MODULE                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                             |  |
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## SYLLABUS

| Hrs | Frontal teaching                                                                                                                                                                                                                                                                                                                                                                                |
|-----|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 4   | Axioms of real numbers. natural, integers and rational numbers. Set theory. Maximum, minimum, supremum and infimum of a set. Uniqueness of the maximum and minimum of a set. Theorem of existence of the supremum and infimum of a set.                                                                                                                                                         |
| 2   | Complex numbers                                                                                                                                                                                                                                                                                                                                                                                 |
| 4   | Functions of a real variable. Surjective, bijective functions. Composte mappings. Monotonic functions. The exponential and logarithmic functions. Powers functions. The circular functions.                                                                                                                                                                                                     |
| 2   | real sequences.                                                                                                                                                                                                                                                                                                                                                                                 |
| 4   | Limitis and convergence of functions. Monotonic functions. Theorems and properties.                                                                                                                                                                                                                                                                                                             |
| 2   | Continuous functions. Discontinuities of a function.<br>Properties and theorems of limits of functions. The intermediate value theorem.                                                                                                                                                                                                                                                         |
| 4   | Differentiation at a point. The chain rule theorem. Differentiation of the inverse mapping. Convex<br>functions.<br>Properties of derivatives functions. Local minimum and maximum. Rolle Theorem. Darboux<br>continuity. The<br>mean value theorem. Taylor theorem with Lagrange and Cauchy remainder. Higher derivatives of<br>order n.<br>Convex functions. L'Hopital rule. Taylor espansion |
| 4   | Integration and elementary integrals. Upper and lower Riemann integrals. Riemann integrable functions.<br>Algebraic property of integrable functions. Mean value theorem. The fundamental theorem of calculus.<br>Change of variable formula. Integration by parts.                                                                                                                             |

| 2   | Numerical series                                        |
|-----|---------------------------------------------------------|
| Hrs | Practice                                                |
| 3   | Exercises on real and complex numbers                   |
| 3   | functions                                               |
| 5   | Exercises on limits of sequences and functions.         |
| 5   | Exercises on continuity and differentiation at a point. |
| 5   | Exercises on integrals.                                 |
| 3   | exercises on numerical series                           |